

MIE-MPI – EXAM				JANUARY 04, 2021	
Name	Q1–6	Q7	Q8	Q9	Σ

Multiple choice question answer table					
Q1	Q2	Q3	Q4	Q5	Q6

Instructions: The questions 1 – 6 have possible answers labelled A–E. There is always exactly one correct answer. Please, use the table above to mark your answer. If you make a mistake, correct your answer in the table (in a readable manner).

Other questions serve as a preparation for the oral part of the exam (nevertheless, your written preparation should be understandable). Don't forget to sign this sheet and all the sheets that you will hand in.

*You can use only a paper, pen and **your** brain! Good luck!*

Question 1 (5 points). Let $f(x, y) = y^3 + xy^2 + x^2y - x$. What is the value of $\frac{\partial^2}{\partial x \partial y} f$ at the point $(-1, 1)$?

- (A) 0
- (B) 2
- (C) $2x + 2y$
- (D) -1
- (E) No other option is true.

Question 2 (5 points). Let us consider as domain D the triangle with vertices the points $(1, 1)$, $(1, 2)$ and $(2, 2)$. Select the value of the double integral

$$\iint_D x + 2y \, dx dy.$$

- (A) 0
- (B) $\frac{1}{2}$
- (C) 2
- (D) $\frac{7}{3}$
- (E) No other option is true.

Question 3 (5 points). Select the **correct** statement

- (A) Every group of order 4 is cyclic.
 - (B) The groups \mathbb{Z}_{12}^\times and \mathbb{Z}_{11}^+ are isomorphic.
 - (C) The group \mathbb{Z}_{12}^\times contains a subgroup of order 4.
 - (D) $P(x) \in K[x]$ is irreducible over a field K if and only if it cannot be decomposed into a product of two elements of $K[x]$.
 - (E) No other option is true.
-

Question 4 (5 points). Let us consider the permutation $f = (5\ 3\ 2\ 7\ 4\ 6\ 1) \in S_7$. The permutation f^6 is:

- (A) (4 1 5 2 6 3 7)
 - (B) (5 3 2 7 4 6 1)
 - (C) (4 2 3 1 7 6 5)
 - (D) (3 2 1 5 4 6 7)
 - (E) No other option is true.
-

Question 5 (5 points). In the field $GF(2^3)$ with multiplication modulo $x^3 + x + 1$, find the inverse of 101.

- (A) 111
 - (B) 100
 - (C) 011
 - (D) 010
 - (E) No other option is true.
-

Question 6 (5 points). Let A and B be two fuzzy sets (over a universe U) having membership functions μ_A and μ_B , respectively. Using the Gödel t-norm for intersection, give the formula for membership function of $A \cup B$.

- (A) $\mu_{A \cup B}(x) = \min\{\mu_A(x), \mu_B(x)\}$
- (B) $\mu_{A \cup B}(x) = 1 - \min\{1 - \mu_A(x), 1 - \mu_B(x)\}$
- (C) $\mu_{A \cup B}(x) = 1 - \mu_A(x)\mu_B(x)$
- (D) $\mu_{A \cup B}(x) = \mu_A(x) - \mu_B(x)$

(E) No other option is true.

*** ORAL PART PREPARATION ***

Question 7. (11 points) Let $f : \mathbb{R}^3 \rightarrow \mathbb{R}$ and $(x, y, z) \in \mathbb{R}^3$. List sufficient conditions for (x, y, z) to be

- (a) a saddle point;
 - (b) a point of local strict minimum.
-

Question 8. (11 points)

1. What is a machine number?
 2. What is the difference between absolute error and relative error?
 3. Discuss about roundoff errors and cancellation errors. Which strategies can we use to minimize them?
-

Question 9. (12 points)

1. Write down the definition of group.
2. Write down the definitions of ring and field.
3. Give an example of a field that is not a ring.