

NIE-MPI, Mathematics for Informatics - Homework no. 1

Instructions:

- You should try to solve all the exercises. Even if you do not do all the exercises, you can get all the points.
 - Presentation is taken into account; correct results themselves are not enough. The reasoning on how the result was found should be clearly visible.
 - Comment your calculations in a reasonable way: the reader should understand what you do and *why*. The solution should be “possible to read”, not “needed to decrypt”.
 - Do not answer unasked questions. It is important to know what is needed to solve the problem and what is not needed.
 - If you use a result from another source than the lectures and tutorials, cite your source properly (do not forget to cite used software if applicable).
 - The homework should be given by hand or sent by email at `dolcefra@fit.cvut.cz` before the beginning of the lecture on Monday October 17th, 2021.
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Exercise 1. Find all minima, maxima and saddle points of the following functions:

(a) $f(x, y) = x^2 - xy + 3y^2$,

(b) $f(x, y) = x^4 - xy + y^4$,

(c) $f(x, y) = \frac{1}{2x} + 3xy$,

(d) $f(x, y) = x^2 \ln x + y^2 \ln y + \sqrt{3}$,

(e) $f(x, y, z) = x^2 + e^{-yz} - yz$.

Exercise 2. Find minima, maxima and saddle points of the following functions:

(a) $f(x, y) = x - y^2$ subject to $\frac{x^2}{4} + y^2 = 1$,

(b) $f(x, y, z) = xy + yz + z$ subject to $xyz = 1$.

Exercise 3. Calculate

$$\iint_D x^2 - y \, dx \, dy$$

where D is equal to:

- (a) $[-1, 2] \times [0, 2]$;
- (b) the triangle with vertices $(0, 0)$, $(1, 0)$ and $(1, 2)$;
- (c) the bounded subset of $(\mathbb{R}^+)^2$ which is delimited by the x -axis, the curve having equation $y = 4 - x^2$ and the line having equation $y = 3x$.